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RESEARCH MEMORANDUM

INVESTIGATION TO DETERMINE EFFECTS OF CENTER-OF-GRAVITY

LOCATION ON THE TRANSONIC FLUTTER CHARACTERISTICS

OF A 45° SWEPTBACK WING

By George W. Jones, Jr., and John R. Unangst

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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

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SUMMARY

An experimental investigation has been conducted in the 26-inch Langley transonic blowdown tunnel to determine effects of center-of-gravity location on the transonic flutter characteristics of a 45° sweptback-wing plan form of aspect ratio 4.0 and taper ratio 0.6. Solid-construction models of the plan form with streamwise NACA 65A004 airfoil sections and center-of-gravity locations at approximately 34 percent chord, 46 percent chord, and 58 percent chord, respectively, were fluttered at several Mach numbers between 0.8 and 1.35.

It was found that, for streamwise Mach numbers from 0.8 to 1.0, the variation with Mach number of the ratio of experimental flutter speed to a calculated incompressible flutter speed was not affected by center-of-gravity location. However, for Mach numbers from 1.0 to 1.35, there was an increase in flutter-speed ratio with Mach number which was different for each center-of-gravity position. Data from wings with successively more forward center-of-gravity locations showed successively larger values of flutter-speed ratio at Mach numbers from 1.0 to 1.35.

INTRODUCTION

As a result of several investigations in the 26-inch Langley transonic blowdown tunnel (refs. 1, 2, 3), extensive data have been obtained which give effects of plan form and Mach number on the flutter speed of swept wings in the transonic speed range. These data have been presented as the variation with plan form and Mach number of a ratio of the experimental flutter speed to a calculated, or reference, flutter speed based on two-dimensional, incompressible aerodynamic coefficients.

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The question arose as to whether the flutter-speed ratios obtained in the previous investigations were functions only of Mach number and plan form or whether the ratios could be affected by changes in some of the elastic and inertia parameters which are present in the calculation of the reference flutter speed. A study of reference 4 suggested that, for the case of a given plan form having low values of the ratio of fundamental bending to torsion frequency, the parameter most likely to affect the variation of the flutter-speed ratio with Mach number was the chordwise location of the center of gravity. An investigation was made, therefore, in the 26-inch Langley transonic blowdown tunnel to determine the effect of the chordwise center-of-gravity location on the variation of the flutter-speed ratio with Mach number.

The plan form used in the investigation had an aspect ratio of 4, sweepback angle of the quarter-chord line of 45°, and a taper ratio of 0.6; and the centers of gravity were located at 34 and 58 percent chord. Results from references 2 and 3 were also available for the same plan form with the center of gravity located at 46 percent chord.

The trends shown by the results of this investigation have been previously discussed and analyzed in reference 5. The flutter-speed ratio at supersonic Mach numbers was shown to be a function of the chordwise center-of-gravity location and a method of analysis was developed therein which credibly explained the effect of the chordwise center-of-gravity location on the flutter-speed ratio.

The purpose of the present report is to present certain details of the center-of-gravity investigation which were not included in reference 5, namely the physical properties of the models used, the values of the test parameters at flutter, and the results of the flutter calculations. For completeness of the present report some of the information from reference 5 is repeated herein.

SYMBOLS

- A aspect ratio including body intercept, Span²
 Area
- a distance in wing semichords from midchord to elastic-axis position; taken perpendicular to quarter-chord line, positive rearward, 2x₀ 1
- Ag geometric aspect ratio, (Exposed span)²
 Exposed area
- b half-chord perpendicular to quarter-chord line, ft

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br half-chord perpendicular to quarter-chord line at intersection of quarter-chord line and wing root, ft

- bs half-chord measured streamwise at intersection of wing root and fuselage, ft
- c wing chord perpendicular to quarter-chord line, ft
- f_{h_i} measured coupled bending frequencies, cps (i = 1 or 2)
- ft measured first coupled torsion frequency, cps
- f_{α} uncoupled first torsion natural frequency relative to elastic

axis, cps
$$f_{\alpha} = f_{t} \left[1 - \frac{\left(\frac{x_{\alpha}}{r_{\alpha}}\right)^{2}}{1 - \left(\frac{f_{h_{1}}}{f_{t}}\right)^{2}} \right]^{1/2}$$

- EI bending stiffness, lb/in²
- GJ torsion stiffness, lb/in²
- gh structural damping coefficient in bending
- I_{α} mass moment of inertia of wing section about elastic axis, slug-ft²/ft
- length of wing panels outside fuselage, measured along
 quarter-chord line, ft
- M Mach number
- m mass of wing per unit length along quarter-chord line, slugs/ft
- q dynamic pressure, lb/sq ft
- r_{α} nondimensional radius of gyration of wing section about elastic axis, $\left(I_{\alpha}/\text{mb}^2\right)^{1/2}$
- V airstream velocity, ft/sec

 V_n component of stream velocity normal to quarter-chord line, ft/sec V_e/V_R flutter-speed ratio, ratio of experimental flutter speed to a calculated reference flutter speed distance, perpendicular to quarter-chord line, of elastic axis $\mathbf{x}_{\mathbf{o}}$ of wing section behind leading edge, fraction of chord center-of-gravity location, fraction of chord behind leading x_{cg} edge, measured perpendicular to quarter-chord line distance in semichords (measured perpendicular to quarter-chord x^{α} line) from wing elastic axis to wing center of gravity, positive when center of gravity is behind the elastic axis nondimensional coordinate along quarter-chord line, fraction of η mass-ratio parameter, $m/\pi \rho b^2$ (values given in table II taken μ at 0.75n) taper ratio. Tip chord/Chord in plane of symmetry λ Λ angle of sweepback of quarter-chord line, deg air density, slugs/cu ft ρ angular frequency of vibration, radians/sec ω angular bending frequency, radians/sec (2πfh;) ω_{hi} angular uncoupled torsion frequency, radians/sec $(2\pi f_{\alpha})$ Φ7. Subscripts: experimental values

MODELS

calculated values

30 - 31 to 15 "

Model Geometry

The plan form selected for these tests had an aspect ratio of 4, a quarter-chord sweepback angle of 45°, and a taper ratio of 0.6. Models

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of the plan form had NACA 65A004 airfoil sections along streamwise chords, a wing span of 1.142 feet, and the ratio of sting diameter to wing span was 0.22.

Two types of models of this plan form were constructed. One type had the center of gravity located at approximately 34 percent chord while the other type had the center of gravity located at approximately 58 percent chord (measurements perpendicular to the quarter-chord line). The models of reference 3, for which data are presented herein for comparison (see table I(b)), had a center-of-gravity location at approximately 46 percent chord. The center-of-gravity locations measured in percent of streamwise chord were 37 percent, 49 percent, and 61 percent. Because of their destruction by flutter, several models of each type were necessary in order to obtain the desired data.

Model Materials and Construction

Figure 1 gives a plan-form view of the three types of models cut away to show the construction details. The models with a center of gravity at 34 percent chord were made with a Compreg (laminated, compressed, resin-impregnated maple) core. These models had a lead-bismuthtin mixture leading edge (50 percent lead, 25 percent bismuth, 25 percent tin by weight) and an outer wrapping of a 0.003-inch-thick Fiberglas cloth. The models with a center-of-gravity position at 58 percent chord were also made with a Compreg core and had a lead-bismuth-tin mixture trailing edge and a Fiberglas wrap. The Fiberglas wrap for the models with 58-percent center-of-gravity location was of three layers; two layers were unilateral Fiberglas cloth (majority of strength in one direction similar to wood grain) with strength directions forming 450 diagonals across the quarter-chord line and the third layer was an outer wrap of 0.003-inch Fiberglas cloth. The lead-bismuth-tin mixture used for leading or trailing edges, was cut perpendicular to the quarterchord line at 1/2-inch spanwise intervals to minimize the effect on wing stiffness. The models of reference 3 which had the same plan form as the models of this report but a location of the center of gravity at 46 percent chord were of solid Compreg wrapped with two layers of 0.003inch Fiberglas cloth, except for one model of plain Compreg with no wrap. On all models the layers of Fiberglas cloth were bonded to each other and to the core with Paraplex cement. The Fiberglas wrapping extended into the wing mounting block at the root for approximately 1/4 inch. The 3/8-inch-thick wing mounting block was an integral part of the wing core of Compreg wood (see fig. 1) and fitted flush in a slot in the '. . . , · The strateging of the contract of sting mount.

Model Physical Parameters

Measurements were made of the following physical parameters on each wing panel of every model tested: (1) elastic-axis position, (2) first and second bending and first torsion coupled natural frequencies, and (3) structural damping coefficient in bending. Measurements were made of the following parameters on at least one wing panel of each type of model constructed: spanwise variation of mass, center-of-gravity location, and mass moment of inertia about the elastic axis (see table I). Measurements made of the spanwise variation of bending and torsion stiffness EI and GJ for a representative panel of each type of model are presented in figure 2. A discussion of the methods used to measure the various physical properties may be found in references 2, 3, and 6.

APPARATUS AND TESTS

The tests were made in the 26-inch Langley transonic blowdown tunnel. A desirable flutter-test feature of this tunnel is that during its operation a selected Mach number which is controlled by an orifice plate can be held approximately constant (after the orifice is choked) while test section stagnation pressure (and thus density) is varied. The tunnel can be operated through the subsonic Mach numbers and up to a supersonic Mach number of approximately 1.45 and the tunnel density range is from approximately 0.001 to 0.012 slug per cubic foot. A more complete description of the tunnel may be found in reference 3.

The flutter-model wings were mounted at 0° angle of attack on a cylindrical sting fuselage. This sting extends into the subsonic flow region of the tunnel and thereby eliminates the formation of a bow shock wave which might reflect from the tunnel walls onto the model. The fundamental frequency of the support system is approximately 15 cycles per second.

Both wing panels of each model were instrumented with wire strain gages. A recording oscillograph was used to give a simultaneous record of the strain-gage signals, tunnel stagnation temperature and pressure, and test-section static pressure. The strain-gage signals were used to indicate the start of flutter and the frequency of wing oscillations.

The tests were conducted in such a manner that the flutter speed and flutter frequency were determined on each model for several Mach numbers throughout the transonic range from about M=0.8 to about M=1.4. A more detailed discussion of the testing technique as well as the model support system and the instrumentation may be found in reference 3.

RESULTS

Method of Analysis

The results of the present tests are presented as the variation with Mach number of a ratio of the experimental flutter speed to a calculated, or reference, flutter speed. The reference flutter speeds for these test results were calculated (as in ref. 3) by use of two-dimensional, incompressible air forces combined with cantilever beam deflection modes in a Rayleigh-type analysis. In the analysis, the mode shape of the wings during flutter was represented by the nondimensional shapes of the first two uncoupled bending modes and the first uncoupled torsion mode of a uniform cantilever beam. The frequencies used in the analysis were the measured values of the first two bending natural frequencies (these values were assumed to approximate the uncoupled values) and the uncoupled value of the first torsion frequency (which was obtained from the measured coupled value by the approximate formula given in the list of symbols herein).

General Comments

Certain general comments made in the section entitled "Results" of reference 3 concerning the nature of flutter encountered and the effects of testing technique apply to the present tests, and may be summarized briefly by the following statements:

- (1) The flutter observed in the tests was of the classical bending-torsion type.
- (2) The amplitude of wing oscillations following the start of flutter did not continually increase with time but increased rapidly to some nearly constant value.
- (3) An easily defined start of flutter was not always obtained. Often, a period of intermittent sinusoidal-type oscillations in both bending and torsion (designated a low-damping region) preceded continuous flutter. In such cases, the exact start of flutter was difficult to pick on the oscillograph record. These cases are treated in the same manner as similar cases in reference 3. Briefly, this involves selecting two data points for those cases in which the exact start of flutter could not be determined. The first point is taken near the beginning of the intermittent sinusoidal-type oscillations and is designated as the start of a low-damping period. The second point is taken near the beginning of continuous flutter and is designated as a point of flutter.

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(4) In some cases, the two panels of the same model did not flutter simultaneously; probably because of slight differences in physical properties between wing panels. In such cases, separate flutter points are presented for the start of flutter for each panel.

(5) The operating characteristics of the tunnel were such that frequently during a single run (a run is defined as one operation of the tunnel from valve opening to valve closing) the tunnel-operating curve of dynamic pressure as a function of Mach number intersected the wing flutter-boundary curve of dynamic pressure required for flutter against Mach number at more than one point. In such cases, each point of intersection is presented in the data.

Presentation of Data

The results of the investigation are tabulated in table II as are some data of reference 3 (table II(b)). The first five columns of the table contain a brief description of the chronological behavior of each wing panel during each run. The first column gives the identification number of the model. A model designation of reference 2 in this column indicates that the data for the run were taken from reference 2 in which no record was kept of the numbers of individual, similarly constructed models of the same plan form. The second column gives the run number, and the third column shows in chronological order the data points which occurred during each run. The fourth and fifth columns contain code letters which describe the behavior of each wing panel at the time of each data point. The code letters and their designations are as follows:

- F flutter
- D low damping
- E end of flutter with dynamic pressure increasing
- N no flutter
- G strain gages inoperative, no record
- X panel destroyed or not installed

Subscripts 1 or 2 attached to these letters indicate the phenomena are related to the first or second occurrence of flutter on the panel during the given run. For example, a series of data points obtained during a given run might be coded as follows:

Donas	Dedast	Wing b	ehavior
Run	Point	Left	Right
3	1	F ₁	F ₁
-	2	El	El
	3	D ₂	D ₂
	4	F ₂	D ₂
	5	F ₂	F ₂

In this example, five data points were obtained during run 3. At the time of point 1, both panels began to flutter and continued to flutter until point 2 when both panels stopped fluttering although the tunnel dynamic pressure was increasing. Then, near the time of point 3 both panels began sinusoidal-type oscillations, designated as low damping, prior to a second occurrence of flutter which became continuous on the left panel near the time of point 4. The right panel continued to exhibit low-damping behavior until point 5 when it too began a continuous flutter for the second time during run 3.

Figures 3 through 6 present the results of the investigation in the form of plots of the ratio of experimental to reference flutter speed Ve/VR as a function of Mach number. Figures 3, 4, and 5 each present the flutter-speed ratios obtained at various transonic Mach numbers on models having one of the three center-of-gravity positions investigated (fig. 4 is data from ref. 3). In these figures, the low-damping periods are indicated by dashed lines beginning at the point selected at the start of the low-damping period and extending to the point of continuous flutter. The data point near the beginning of a low-damping period is denoted by the lower end of the dashed line whereas the data point near the beginning of continuous flutter is marked by a symbol. The path of the dashed lines is a function of tunnel operating conditions as the flutter point was approached. The points at the start of flutter are indicated by plain symbols and points at the end of flutter are indicated by shaded symbols, Figure 6 is a plot which superimposes the three faired flutter boundaries of figures 3, 4, and 5.

DISCUSSION

As may be observed in figure 6, the flutter-speed ratios for the three center-of-gravity positions merged in the high subsonic range (0.8 \leq Me \leq 1.0) with values near 1.0. Thus, in the high subsonic range, the reference flutter speed accurately predicts the experimental flutter speed. In the low supersonic range (1.0 \leq Me \leq 1.35), there is a rapid increase in Ve/VR as the Mach number increases, but the rate of increase is different for the various center-of-gravity positions so that each configuration has a separate flutter boundary. Examination of figure 6 shows that the rate of increase of Ve/VR with Mach number becomes larger as the center of gravity moves forward. Thus, for the test plan form in the supersonic speed range investigated, the flutter-speed ratio is not a function of plan form and Mach number alone but also appears to be a function of center-of-gravity position.

Some doubt may be expressed that the difference in the V_e/V_R curves in figure 6 should be attributed to chordwise changes in center-of-gravity location because, as previously stated, models of the present investigation which had different center-of-gravity locations also had different values of the elastic and inertia parameters $\omega_h/\omega_{\rm L}$, $r_{\rm C}$, m, and a. It can not be proved from the available data that the differences in the V_e/V_R curves were not affected by the changes in these other parameters. However, on the basis of the analysis in reference 5 which uses trends and conclusions drawn in reference 4, the chordwise center-of-gravity location would appear to be the major factor in accounting for the present differences in the supersonic values of the flutter-speed ratios.

The flutter data as presented in figure 6 cannot indicate directly the relative flutter susceptibility of a given wing design as the center of gravity is moved, since both $V_{\rm e}$ and $V_{\rm R}$ would be expected to change. However, it can be shown with the aid of a comparison of the sharp upsweep of the curve of $V_{\rm e}/V_{\rm R}$ for the 34 percent chord center-of-gravity location with the more gentle upsweep of the curves for the 46- and 58-percent-chord locations that it may be possible to reduce the severity of the flutter problem at supersonic speeds by a suitable forward location of the center of gravity.

In the subsonic speed range the curves of $V_{\rm e}/V_{\rm R}$ in figure 6 are the same for all center-of-gravity locations tested and thus do not reveal the fact that the actual flutter speeds vary with the center-of-gravity location. Nor can the effects of center-of-gravity location on the flutter speed be obtained by directly comparing the experimental flutter

speeds because the models constructed with different center-of-gravity locations had necessary differences in mass and stiffness parameters which affect the flutter speed. However, an examination of the nondimensional flutter-speed coefficient $V_{\rm R}/b_{\rm r}\omega_{\rm r}$ given in table II shows that,

for equal values of mass ratio, the flutter-speed coefficients at subsonic speeds had approximately a 25-percent increase as the center of gravity shifted from 0.58 chord to 0.46 chord and an additional increase of approximately 75 percent as the center of gravity shifted from 0.46 chord to 0.34 chord. These increases in $V_R/b_R\alpha_L$, which were based on three-dimensional calculations to the extent that spanwise variations of mass, geometry, and airfoil vibration mode shape were taken into account, are similar to those shown by the calculations of reference 4 for a two-dimensional wing.

CONCLUSIONS

The conclusions drawn from an experimental investigation of effects of center-of-gravity location on the transonic flutter characteristics of a 45° sweptback wing follow:

- 1. For streamwise Mach numbers from 1.0 to 1.35, the flutter-speed ratio was affected by center-of-gravity changes. In this Mach number range, there was an increase in flutter-speed ratio (ratio of experimental to calculated flutter speeds) with Mach number which was different for each center-of-gravity position. The rate of this increase in flutter-speed ratio became larger as the center of gravity moved forward.
- 2. For streamwise Mach numbers from 0.8 to 1.0, presenting the results as a flutter-speed ratio removed the effect of center-of-gravity position since the flutter-speed ratio was approximately 1.0 in this range for all center-of-gravity positions tested.

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3. The calculated flutter-speed coefficients for equal values of mass density ratio, increased approximately 25 percent when the center of gravity was changed from 0.58 chord to 0.45 chord and increased approximately an additional 75 percent when the center of gravity was changed from 0.45 chord to 0.34 chord.

Langley Aeronautical Laboratory,
National Advisory Committee for Aeronautics,
Langley Field, Va., October 15, 1955.

REFERENCES

- 1. Bursnall, William J.: Initial Flutter Tests in the Langley Transonic Blowdown Tunnel and Comparison With Free-Flight Flutter Results. NACA RM L52K14, 1953.
- 2. Jones, George W., Jr., and DuBose, Hugh C.: Investigation of Wing Flutter at Transonic Speeds for Six Systematically Varied Wing Plan Forms. NACA RM L53GlOa, 1953.
- 3. Unangst, John R., and Jones, George W., Jr.: Some Effects of Sweep and Aspect Ratio on the Transonic Flutter Characteristics of a Series of Thin Cantilever Wings Having a Taper Ratio of O.6. NACA RM L55113a, 1955.
- 4. Theodorsen, Theodore, and Garrick, I. E.: Mechanism of Flutter A Theoretical and Experimental Investigation of the Flutter Problem. NACA Rep. 685, 1940.
- 5. Loftin, Laurence K., Jr.: Flutter Characteristics of Swept Wings at Transonic Speeds. NACA RM L55E19a, 1955.
- 5. Land, Norman S., and Abbott, Frank T., Jr.: Transonic-Flutter Investigation of a Fighter-Airplane Wing Model and Comparison With a Systematic Plan-Form Series. NACA RM L55Bl6, 1955.

TABLE I.- PHYSICAL PROPERTIES OF MODELS

(a) Wings with center of gravity at approximately 34 percent chord

Parameter	Wings 1, 2, 3, 4, and 5
NACA section A A, deg \(\lambda \), ft Span, ft Ag 1, ft br, ft bg, ft Average xc.g.	654004 4 145 0.6 0.657 1.142 1.65 0.630 0.123 0.163 0.337 0.0214

	WI	ng No. 5	(left per	el)
η 	×α	B.	r _a ²	m, slugs/ft
0.05 0.05 0.05 0.05 0.05 0.05 0.05 0.05	-0.305 321 337 352 368 383 398 414 429 444	0.028 .035 .047 .054 .060 .067 .074 .081 .087	0.465 .457 .450 .442 .441 .487 .504 .513 .516	0.00899 .00869 .00835 .00793 .00737 .00625 .00568 .00518 .00475

,	Wing N	0.1	Wing N	ю. 2	Wingl	¥o. 3	Wing N	io. 4	Wing N	io. 5
Frequency	Left Panel	Right panel								
f _h	61	61	61	60	- 60	65	64	61	61.	61
r _{h2}	332	322	31ب2	327	322	361	<u>ت</u> ہاد	322	318	331
$^{\mathtt{f}}\mathtt{t_{1}}$	210	208	226	230	232	228	227	213	217	218
\mathbf{r}_{a_1}	173.2	172.4	187	191	192	188	188	176	179.3	180
$(\omega_{n_1}/\omega_{\alpha_1})^2$	0.1240	0.1252	0.1062	0.0995	0.0977	0.1172	0.1163	0.1200	0.1150	0.1146
$(\omega_{\rm h_2}/\omega_{\alpha_1})^2$	3.6743	3.4885	3.3484	2.9465	2.8126	3.6716	3.3005	3.3663	3.1455	3.3740

TABLE I.- Continued

(b) Wings with center of gravity at approximately 16 percent chord

Parameter	Wing of Ref. 2 Wings 1 and 2
A. deg Panel \(\lambda\) Span, ft Ag 1, ft br, ft ten, ft Average xog gh	65A004 45 0.657 1.142 1.65 0.630 0.123 0.163 0.455 0.030

		Wing of	Ref. 2		Wing no. 1								
η	x _a a r _a ² sh				$\mathbf{x}_{\mathbf{a}}$	a	ra ²	m, slugs/ft					
0.05 .15 .25 .35 .45 .65 .75 .85 .95	-0.02 .01 .04 .07 .09 .12 .15 .17 .20	-0.07 10 15 18 21 24 26 29 32	0.22 .22 .23 .24 .25 .26 .26 .27	0.00561 .00527 .00493 .00458 .00424 .00389 .00355 .00321 .00286	0.037 .030 .023 .016 .009 .002 005 012 018 025	-0.117 110 102 095 088 082 074 067 060 053	0.233 .234 .235 .236 .237 .238 .239 .240 .241	0.00733 .00648 .00576 .00516 .00472 .00435 .00407 .00382 .00361					

	Wing of Ref. 2	Wing h	No. 1	Wing 1	No. 2	
Frequency	Both panels	Left panel	Right panel	Left penel	Right panel	
$\mathbf{f_{h_1}}$	88	67	64	78	73	
$\mathbf{f_{h_2}}$	462	357	367	399	387	
$\mathbf{f_{t_1}}^-$	370	356	3կ2	389	378	
$\mathbf{f}_{\mathbf{\alpha}_{\mathbf{l}}}$	361	356	342	389	378	
$(\omega_{\rm h_1}/\widetilde{\omega}_{\alpha_1})^2$	0.0594	0.0354	0.0350	0.0402	0.0373	
$(\omega_{\text{h}\underline{1}}/\widetilde{\omega}_{\alpha_{\underline{1}}})^2$ $(\omega_{\text{h}\underline{2}}/\omega_{\alpha_{\underline{1}}})^2$	1.638	1.006	1.151	1.053	1.049	

TABLE I.- CONCLUDED

(c) Wings with center of gravity at approximately 58 percent chord

Parameter	Wings 1, 2, 3, 4, and 5
NACA section	65A004
A	4
Λ , deg	45
λ	0.6
Panel \(\lambda\)	0.657
Span, ft	1.142
$\mathbf{A_{g}}$	1.65
l, ft	0.630
b _r , ft	0.123
b _s , քե	0.163
Average x _{cg}	0.5795
8h	0.0327

·	¥	fing No. 3	(right p	anel)
η	×α	a	ra ²	m, slugs/ft
0.05 155 345 555 785 95	0.061 .074 .086 .098 .111 .123 .135 .148 .160	0.099 .086 .074 .062 .049 .036 .024 .011 001	0.226 .241 .252 .259 .260 .255 .258 .273 .284	0.01176 .01161 .01093 .01040 .00951 .00618 .00732 .00660 .00598

	Wing l	No. 1	Wing l	No. 2	Wing 1	No. 3	Wing 1	No. L	Wing No. 5		
Frequency	Left panel	Right panel	Left panel	Right panel	Left panel	Right penel	Left panel	Right panel	Left panel	Right panel	
f _{hl}	48 51 50 50				49	51.	51	52			
$\mathbf{f_{h_2}}$	1 . 1 . 1		247	247 247		235	238	236	226	230	
f _{t1}	382	382	385	385	380	383	· 391	386	363	360	
f _{al}	371.6	371.6	374.6	374.6	370	373	380	376	353	350	
$(\omega_{h_1}/\omega_{\alpha_1})^2$	a. 01668	0.01883	0.01781	0.01781	0.01764	0.01888	0.01833	0.01808	0.02129	0.02104	
$(\omega_{\rm h_2}/\omega_{\alpha_1})^2$	0.4347	0.4709	0.3437	0.3437	0.3870	0.3878	0.3917	0.3949	0.40965	0.4313	

TABLE II .- CONTILATION OF AMAINTICAL AND EXPERIMENTAL RESULES

Wing penel behavior code: F - flutter

E - cad of flutter (dynamic pressure increasing)

I - no flutter 0 - strain gages not working

Subscripts: 1 - associated with first occurrence 2 - associated with second ecourement of flatter during the run of flatter during the run

(a) Hings with center of gravity at approximately 3k percent chord

	_	44	Wine 1	Dehavior												<u> </u>		
Model	Rain	Paint	Left	Might	¥* .	V₀/V R	Pa sluga/on fo	μ,	/ ≒	redians/sec	- g∕o _t	radiama/sec		fi/am	r√R ••••	Ve/bras	All	1₽\1₽ ₅
44444	1 2	1 2 3 1 2	eleterete	मान्य वास्त्राज्ञ	988899	1.146 1.017 1.101 1.147 1.054 1.228	0.003h .0022 .0021 .0081 .0023	58.11 89.88 91.88 91.88 91.88	7.62 9.18 9.70 9.70 9.27 9.27	1063.2 1063.2 1063.2 1063.2 1063.2	0.6713 .6369 .6368 .6362 .635	772.8 628.3 	1.063 .907 .939	867.5 933.7 1025 1072.1 950.8	772.6 917.7 930.9 935.1 901.8	6.6l/6 7.008 7.729 8.0l/9 7.136	5.80 6.89 7.02 7.02 6.17	1333 959 1103.2 1207.5 1059.6
22228	4 5 6 7	1 2 1 1 1 2	ೆ ಗೆಂದರಗೆಗ	i nericke	5.55 5.55 5.55 1.13 1.13	1.075 1.101 1.099 1.066 .997 1.161	-0055 -0055 -0055 -0055 -0055 -0055	82.32 82.32 79.62 82.32 89.80 89.80	9.07 9.07 8.89 9.07 9.48 9.48	1083.2 1083.2 1083.2 1083.2 1083.2 1185.6 1185.6	.61.68 .61.68 .61.68 .61.68 .63.98	634.6 517.2 517.2 672	· 1 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	973.8 977.1 998.5 946.9 1000.7 1164.6	901.8 887.1 887.1 872.5 887.1 1005.3 1008.3	8.313 7.159 7.334 7.194 7.110 6.862 7.966	6.77 6.666 6.666 6.688 6.688 6.688	1091.7 1116.7 116.5 1073.7 1161.5 1191.9
22000	8 9	12123	P1	<u>ಗೆಜೆಲೆಗೆ</u> 00	.956 1.659 1.672 1.713 1.713	1.000 1.057 .909 1.175 1.140 1.140	.0033 .0034 .0040 .0400	85.90 85.90 82.32 75.98 19.39	9.27 9.27 9.07 8.72 7.03 6.70	185.6 185.1 185.1 185.1 185.1	.6134 .6134 .6527 .6527 .6533	679 766 ————————————————————————————————	.890 .991 	997.5 1142.6 909.9 1113.9 1153.4 1150	967.3 967.3 979 968.1 801.1 773.2	6.850 7.834 6.190 7.578 7.866 7.823	6.77 6.43 6.43 6.43 6.43 6.43 6.43 6.43 6.43	1114.3 1500.8 993.5 1613 2660.7 2909.5
"	10	3 1 2 3	No. No. No. No.	X X X X X X X X X X X X X X X X X X X	.88 1.63 1.15 .83 1.63 1.11	1.059 1.167 1.195 1.026 1.160 1.137	.0025 .0025 .0065 .0026 .0086	79.02 79.02 13.90 82.32 75.90	8.89 8.69 6.63 9.07 8.72 7.03	1206.h 1206.h 1206.h 1206.h 1206.h	859 859 850 850 850 850 850 850 850 850 850 850	160 1005 729 986	.970 1,211 .934 1,200	128.9 124.8 129.5 129.6 129.5 129.5	971.9 971.9 174.6 968.3 957.1 868.7	6.934 7.885 7.885 7.894 7.894	6.55 6.55 6.55 6.45 6.45	1323.3 1573.5 3018.7 1232.9 1602.9 2702.8
	13 14	12 11 11	Hallende	たがみがだけ	110000 1100000 11000000000000000000000	1.055 1.154 1.362 1.379 1.028 1.044	.602) .0027 .0033 .0036 .0030	82.32 73.27 59.67 56.65 65.65 73.27	9.07 8.77 7.11 8.57	1111.0 1111.0 1111.0 1111.0 1111.0	.668 .659 .669 .6132 .6628 .6555	767 989 930 751 761	1.039 1.213 1.211 997 991	986.5 1117.7 1121.8 1110.5 678.4 930.7	934.7 891.2 823.8 805.6 854.7 891.2	7.089 7.994 7.993 7.913 6.299 6.632	6.66 6.33 5.87 5.74 6.09 6.35	1167.8 1686.5 2016.4 2145.8 1157.1 1169.4
HANNEN	15 16 17 18	1 1 2 1 2	51 0 H Sil 51 51	かんかあれる	.891 .908 .936 1.128 .875 1.053	1.0k3 1.0k9 1.0k9 1.222 1.007 1.199	.0054 .0053 .0053 .0053 .0052	79.02 85.90 89.80 89.80 85.90 83.91	8.89 9.27 9.18 9.18 9.27 9.27	1111.0 1129.7 1129.7 1129.7 1129.7	.64,96 .63,96 .63,96 .63,96 .64,94 .64,66	7144 7259 707 672	1.00h .575 .576 .555	958.6 971.8 1002.5 1167.9 947.1 1110.1	919.2 950.1 956.0 956 940.7 925.4	6.830 6.925 7.215 8.505 6.816 7.989	6.55 6.77 6.56 6.56 6.77 6.66	1148.6 1086.1 1105.5 1500.4 1011.5 1478.8

^{*} Run - A run is defined as one operation of the blosdown tunnel from welve opening to valve closing.

^{70%} Point - Chronological order in added recorded points economic during the test run.

TABLE II.- Continued

(b) Nings with center of-previty position at approximately has-percent

												■R.	** .	- ₄ /- ₂	٧.	v _R	∀ _/0 <u>,44</u> 0	Va/byee	9.
Model	Rama	Podni	Left	Marior	ц	v. ∕∨ <u>p</u>	eluga/cu fi	μ	₽ ₽₀	redians/sec	- Cap√a -c		redians/see	~~	14√s∞	ft/sea			16/ft ²
(Ref.2)	127476	1111111	たけなれたな	Spirital Spirits	288842 288842	1.032 1.039 1.036 1.030 1.047 1.062	0.0033 .0030 .0086 .0028 .0026 .0027	17.19 13.72 13.68 14.68	6.09 6.28 6.61 6.61 6.86 6.73	2268 2268 2268 2268 2268 2268	20000000000000000000000000000000000000	1201.5 1200.9 1170.3 1170.3 1175.5 1163	10k7 10k7 995 995 958		805.1 795.6 856.0 850.7 867.7 868.8	780.4 765.8 825.8 825.8 845.1 837.0	2.88 2.85 3.04 3.18 3.19	2.50 2.75 2.56 2.56 3.04 3.00	1070 961 1036 1013 1024 1067
*****	7	12761	N Dink	. ಇನ್ನುಗಳು	1.3% 1.3% 1.3% 1.350 1.023 1.023	1,587 1,641 1,800 1,830 1,095 1,614	.0029 .003, .0068 .0074 .0081 .0083	2.21 25.50 25.67 25.67 25.88	6.50 5.75 7.75 7.75 7.75	2268 2268 2268 2268 2268 2268	.5322 .5322 .5359 .5459 .5502	1177.5 1207 1263 1279.8 1104.5 1202.4	15% 15% 15% 15%	1.313 1.371 1.013 1.281	1896.7 1267.8 1215 1214.8 1011 1256	817.4 172.7 675.1 663.9 923 778	1.65 1.55 1.36 1.36 1.56 1.50	2.92 2.77 2.52 2.38 3.32 2.79	21,38.8 2732.h 2666.7 3981.5 1073 2603
	9 10 11 12	1 1 1 2	われたから	194711	975 1 301 975 914 774	1.124 1.500 1.125 1.052 .972 1.020	.0024 .0031 .0025 .0026 .0026 .0027	51.23 35.99 47.05 47.05 47.05	7.16 6.24 7.05 6.66 6.61 6.73	2268 2268 2268 2268 2268 2268 2268	5036 955 5047 5056 1060	1137.6 1191.8 1181.6 1195.5 1170.3 1163.0	1121 2023 1010 1063 1162	.985 .894 .900 .906 .999	901 1274 973 921 803.3 854	873 795 865 875 825,8 837	3.50 1.38 3.48 3.30 2.88 3.06	3.13 2.5k 3.10 3.0h 2.96 3.00	1155 2322 1163 1103 903 905
1 1 1	13 14 15	1 2 1 2 1 2	N N N N N N	กลายกล	.961 1.352 .950 1.039 .862 1.059	1.129	.0022 .0035 .0018 .0017 .0019	55.61 34.98 80.93 85.69 76.67 85.69	7.16 5.92 9.26 9.26 8.76 9.26	2268 2268 2148.8 2148.8 2148.6 2148.6	1978 1912 1019	1120 1212 663.6 676.3	1696 1417 859 859 856 856	.976 1.295 -995 -960	9% 1223 977 1662 906 1073	901.1 751.1 922.1 910.9 901.3 910.9	3.42 4.38 3.69 4.41 3.41 3.60	3,82 2,74 3,19 3,56 3,11 3,56	1005 2618 860 942 768 100k
1 1 1 1 1	17	1 2 3	F1 0 0 0 71	n id divis	.571 1.179 1.292 1.292	1.707 1.707 1.761	.007	60.70 77.56 39.37 36.34 96.00	6.27		.1525 .1713 .1736 .1408	989.3 1012.7 1017.7 984.6	919 919 11,60 982	.968 1.335 .997	562 1183 1217 1233 579	867.5 865.4 713.6 707.3	3.27 1.60 1.66 3.19	3.1k 3.35 2.70 2.68 3.06	922 1536 2753 2820 996
2 2 2 2 2 2	18 19 20	1 2 1 2 1 2	ひたかからか	0 0 0	1.31 1.31 1.21 1.19 1.20 1.18	1.712	.0019 .0053 .0037	35.53 29.72 10.15 39.37 14.35 37.33	6.64 6.64 6.64	2144,2 2144,2 2144,2	.h725		1591 1302 1353	1.322	1269 1271 1200 1173 1192 1166	784.7 71,2.6 811.7 811.7 814.8	1.29 1.23 1.00 3.90 3.96 3.88	2.61 2.h7 2.81 2.70 2.81 2.68	3411 3979 2388 2537 2326 2628
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2)	1 1 2 1 9		o einings	.836 1.307 1.333 .883 1.349 1.28	1.600 1.680 900 1.183 1.928	.0077 .0044 .0022 .0022	98,27 39,37 33,11 66,21 72,61 14,15 36,31	6.27 5.77 6.11 6.61	2375 2110 2110 2110	. 1,366 . 1,713 . 1,616 . 1,237 . 1,618 . 1,736	1119.5	900 1539 905 — 1495	1.337 1.337 1.886 1.329	设建。7	993	3.32 h.32 h.27 3.17 3.96 h.29 h.26	3.09 2.70 2.57 3.25 3.35 2.68	110h 29h6 35; 971 1378 2995 2949
2 2 2 2	21a 25 26	1 1 2 3 4 1	たれないかれ	n n n n n n n n n n n n n n n n n n n	.85 .90 1.00 1.1k 1.17	1.03 1.03 1.15 1.15 1.25	7 .0028 3 .0028 4 .0023 2 .0026 5 .0026	93.00 60.10 63.33 96.00 93.00 93.20	7.7: 7.9: 7.4: 7.2:	2110 2110 211112	.1479 .1386 .1400 .1479 .1436	1142.6 1075.9 1093.8 1067.4	956 930 — 1115 892	.885 .892 — 1.013 .836	1116.3 1166.1 1166.1 926.3	931 943 920 892.9 929	2.05	2.97 3.14 3.18 3.06 2.97 3.09	1166 1109 1132 1696 1905 1072
2 2 2 2 2 2 2 2 2 2	27 28 29 30	1 2 1 2 1	たいかいれたれ	a a a a a	.92 1.05 1.21 1.21 .81 .87	1.09 1.69 9 1.90 6 .96	7 .0021 0 .0035 8 .0039 0 .0021	66.26 69.37 51.66 37.37 60.76	6.1 6.1 6.1 7.7	3 21.14.2 21.14.2 21.14.2 21.14.2	166 175 175 175 175 175 175 175 175 175 175	1110.2 1162.2 1056.9	131.5 886 896	1.157 .838 .850	1005.3 1199.2 1201.6	969.3 826.6 796.7	3.61	3.2h 3.29 2.65 3.1h 3.1h	1030 1237 2517 2615 965 1052

TABLE II.- Concluded

(c) Wings with center of gravity at approximately 58 percent chord

Kodol	Run	Point	Wing Be	bavior	μ _e	v./v _R	Po aluga/om ft	μe	√H•	ω _α radiana/sec	osp/os _{cs}	e _R radiana/seo	o _e redians/sec	eco/ecg	V _e ft/sec	Vg ft/sec	Ve/braa	Vp∕orcea	40 1b/ft ²
		rount	Left	Right															
33333	1971100	1 1 1 1 1	がなみがだれ	ひ むひだなん	1.38.85.65 5.39.88.65	1.509 1.059 1.058 1.053 1.076 1.029	0.0034 .0000 .0022 .0027 .0030 .002\$	73.96 62.87 114.31 93.14 83.83 100.59	8.60 7.93 10.69 9.65 9.16 10.03	2334.8 2773.0 2332.0 2332.0 2332.0	0.3kg3 .3510 .3067 .323k .3333 .3172	794.5 825.9 715.2 754.2 772.6 739.7	1131 905 691 785 823 741	1.124 1.096 .966 1.011 1.065 1.002	1253.3 863.1 1005 928 924 926	830.5 803.4 932.5 881.2 857.1 899.8	1.361 3.051 3.504 3.235 3.221 3.228	2.892 2.776 3.251 3.072 2.988 3.137	2670.3 1559.7 1111 1157.1 1280.7 1071.8
3 3 3 3	7 8 9	1 2 3	71 71 71 71 71 71 72	. o o o	.936 .962 1.179 1.306	1.00 1.00 1.06 1.06 1.23 1.128	*005/ *0050 *0010 *0050	119.75 119.75 125.74 132.36 104.78	10.94 10.94 11.21 11.50 10.44	2332.0 2332.0 2323.0 2323.0 2323.0	.3025 .2934 .2935 .3139	705.4 705.4 692.7 681.6 729.2	71.0 70k 71.0 980	1.007 .998 1.025	985 991 1014 1193 1290	954.6 954.6 968.3 966.9	3.434 3.455 3.549 4.175 4.515	3.294 3.294 3.341 3.369 3.174	1038.6 982.1 1028.2 1352.0 1996.9
33354444	10	1 2 3 1 2 3 . 4		0 0 0 0 PH 100 FT	.550 1.223 1.300 .511 .566 1.169 1.265	1.067 1.287 1.400 1.047 1.059 1.25h 1.365 1.395	.0021 .0020 .0023 .0021 .0021 .0021 .0024	119.75 125.74 129.75 119.75 119.75 119.75 119.75	10.9h 11.11 10.16 10.9h 10.9h 10.9h 10.2h 9.83	2323.0 2323.0 2323.0 2323.0 2375.7 2376.7 2376.7 2376.7	.3025 .2962 .3103 .3025 .3025 .3025 .3139 .3205	702.7 692.7 720.8 702.7 718.3 718.3 715.4 761.1	70k 968 70h 766 1005	1.002 1.3k3 1.002 1.066 	1004 1228 1228 1228 1019 1206 1265 1264	961.2 956.3 917.8 961.2 962.1 962.1 962.1 906.2	3.514 4.298 4.497 3.147 3.1489 4.331 4.328	3.29h 3.340 3.29h 3.29h 3.29h 3.17h 3.103	1008 1508 1898.9 1038.1 1050.3 1527.2 1920.3 2077
444555	13 14 15 16 17	1 1 1 2	がなれなが	e Selection of the selection of the sele	855 855 855	1.050 1.013 1.007 1.105 1.006 1.333	.0050 .0050 .0051 .0051	104.78 125.74	10.02 10.24 10.24 11.21 11.21	2374-7 2374-7 2374-7 2209-5 2209-5 2209-5	.1172 .1172 .1139 .1139 .2982 .2982	753.3 753.3 745.4 693.6 658.9 658.9	761 729 729 716 691	.968 .968 .978 1.032 1.069	962 928 934 953 953 954	916.3 916.3 927.1 862.6 907.7	3.254 3.177 3.190 3.507 3.652 4.452	3.137 3.137 3.174 3.174 3.340 3.340	1156.8 1076.5 1066.8 1089.8 968.3 1464.1
5	16	3	7 ₂	P ₂ P ₁		1.648 1.667	.0023	109.3h 111.31	10.16 10.69	2209.5 2209.5	.3103 .3067	695.6 677.7	993 722	1.446 1.065	126k 9k3	β72.9 883.5	4.651 3.470	3.212 3.251	1837.h 978.2

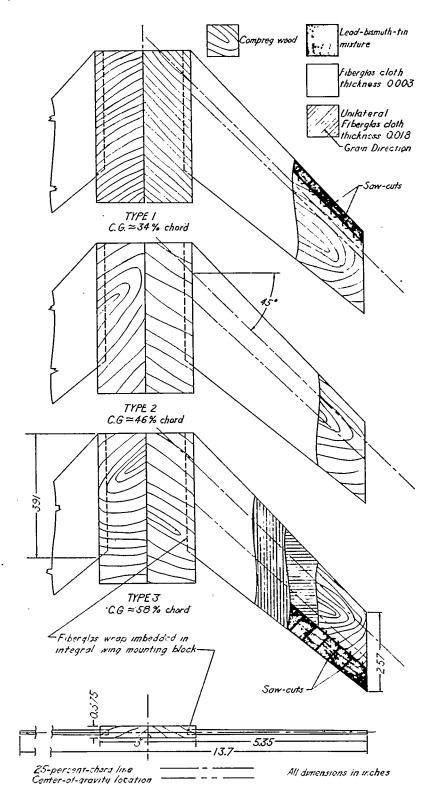


Figure 1.- Cutaway plan-form view of the three types of models showing construction used to vary the center-of-gravity location.

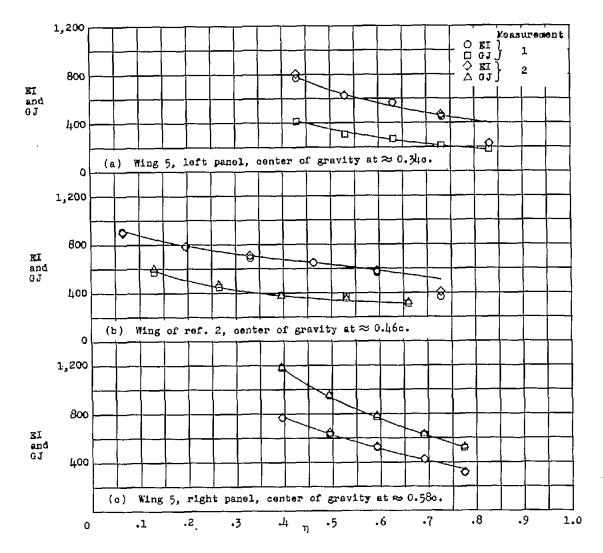


Figure 2.- Typical spanwise stiffness measurements on three models, each having a different center-of-gravity location.

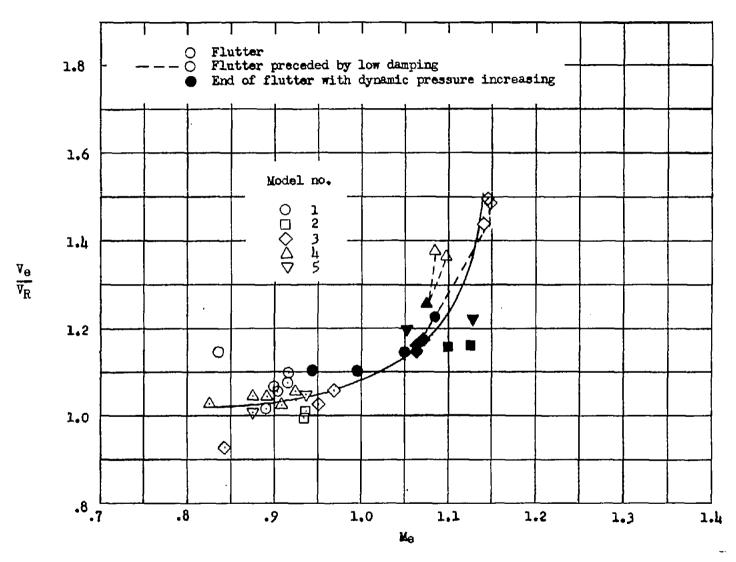


Figure 3.- Variation of flutter-speed ratio with Mach number for models with center-of-gravity locations at approximately 34 percent chord.

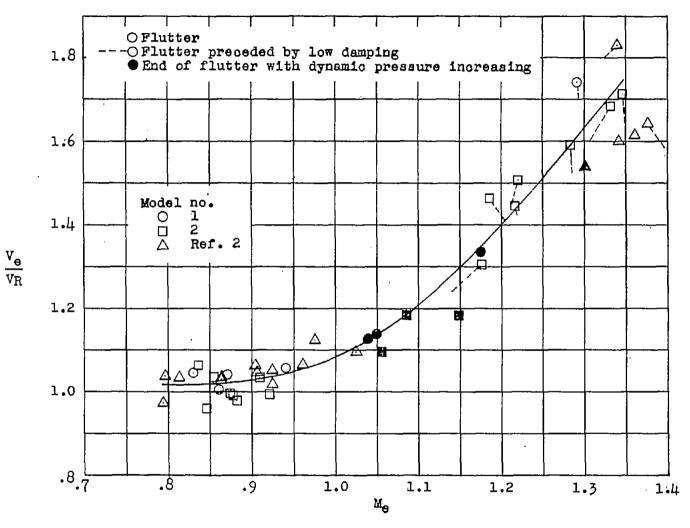


Figure 4.- Variation of flutter-speed ratio with Mach number for models with center-of-gravity locations at approximately 46 percent chord. (Data from ref. 3.)

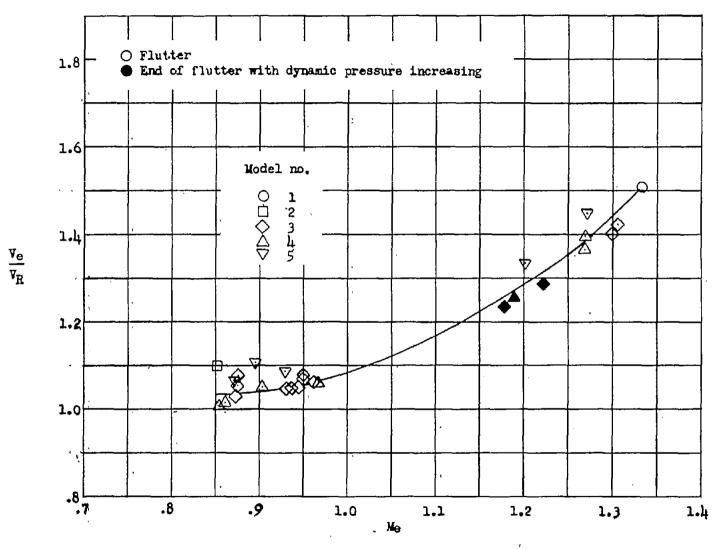


Figure 5.- Variation of flutter-speed ratio with Mach number for models with center-of-gravity locations at approximately 58 percent chord.

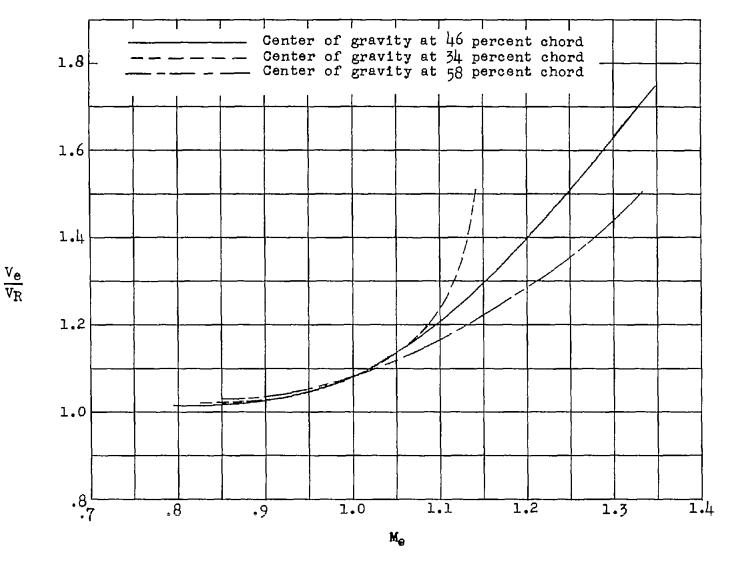


Figure 6.- Effect of center-of-gravity location on the variation of the flutter-speed ratio with Mach number.

NACA - Laughey Field, Va.